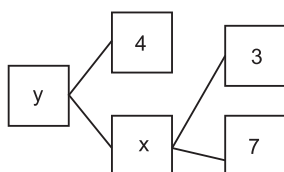


Solutions to RSPL/3 (Basic)

1. (b),



$$x = 7 \times 3 = 21$$

$$y = 4 \times 21 = 84$$

\therefore Option (b) is correct.

2. (c),

$$\begin{aligned} f(x) &= (x - 2)^2 + 4 \\ &= x^2 + 4 - 4x + 4 \end{aligned}$$

$$f(x) = x^2 - 4x + 8$$

$$a = 1, b = -4, c = 8$$

$$\begin{aligned} D &= b^2 - 4ac \\ &= (-4)^2 - 4 \times 8 \\ &= 16 - 32 = -16 < 0 \end{aligned}$$

The given equation have no zero

\therefore Option (c) is correct.

3. (c), diameter of larger wheel = 50 cm

$$\text{Radius of larger wheel} = \frac{50}{2} = 25 \text{ cm}$$

$$\text{Circumference of larger wheel (1 revolution)} = 2\pi r = 2\pi \times 25 \text{ cm} = 50\pi \text{ cm}$$

$$\text{Distance travelled in 15 revolutions} = 15 \times 50\pi = 750\pi \text{ cm}$$

$$\text{Diameter of smaller wheel} = 30 \text{ cm}$$

$$\text{Circumference of smaller wheel} = 2\pi(15) = 30\pi \text{ cm}$$

Number of revolutions made by smaller wheel

$$= \frac{\text{Total distance travelled by larger wheel}}{\text{circumference of smaller wheel}}$$

$$= \frac{750\pi}{30\pi} = 25$$

\therefore Option (c) is correct.

4. (c), Let α and β are roots of the quadratic equation $x^2 + bx + 1 - b = 0$,

Such that $\alpha = 1 - b$

$$\alpha + \beta = \frac{-b}{a} \text{ and } \alpha\beta = \frac{c}{a} = \frac{1-b}{1}$$

$$\alpha \cdot \beta = 1 - b$$

$$\Rightarrow (1 - b)\beta = (1 - b)$$

$$\Rightarrow \beta = 1$$

$$\begin{aligned}\alpha + \beta &= -b \\ 1 - b + \beta &= -b \\ \beta &= -1\end{aligned}$$

Roots are $(1, -1)$

\therefore Option (c) is correct.

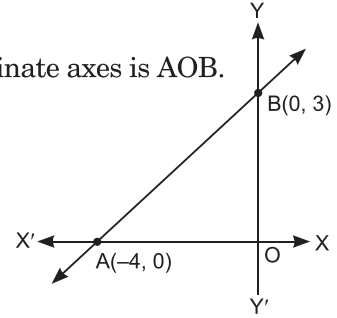
5. (d), \therefore Probability of sure event is always 1.

6. (a), as

Let the triangle formed by line $3x - 4y + 12 = 0$ with coordinate axes is AOB.

A(-4, 0) B(0, 3) O(0, 0)	<table style="border-collapse: collapse;"> <tr> <td style="padding: 2px 10px;">x</td> <td style="padding: 2px 10px;">0</td> <td style="padding: 2px 10px;">-4</td> </tr> <tr> <td style="padding: 2px 10px;">y</td> <td style="padding: 2px 10px;">3</td> <td style="padding: 2px 10px;">0</td> </tr> </table>	x	0	-4	y	3	0
x	0	-4					
y	3	0					

$$\begin{aligned}\text{Area of } \triangle AOB &= \frac{1}{2} |-4(3 - 0) + 0(0 - 0) + 0(0 - 3)| \\ &= \frac{1}{2} |-12| = 6 \text{ unit}^2\end{aligned}$$



\therefore Option (a) is correct.

7. (c), $n = 31, a_{16} = m$

$$\begin{aligned}a_{16} &= a + 15d = m \\ s_{31} &= \frac{31}{2} [2a + (31 - 1)d] \\ &= \frac{31}{2} [2a + 30d]\end{aligned}$$

$$\Rightarrow = \frac{31}{2} \times 2(a + 15d) = 31m$$

$\Rightarrow \therefore$ Option (c) is correct.

8. (d), Two lines in the plane either intersect or are parallel.

\therefore Option (d) is not possible.

9. (c), Cost of each pen is ₹ x , cost of each pencil is y

$$\text{cost of 3 pens and 5 pencils} = 3x + 5y = 40$$

$$\text{Cost of 5 pens and 4 pencils} = 5x + 4y = 58$$

\therefore Option (c) is correct.

$$\begin{aligned}10. (b), & \frac{\cos x}{1 - \tan x} + \frac{\sin x}{1 - \cot x} \\ &= \frac{\cos x}{1 - \frac{\sin x}{\cos x}} + \frac{\sin x}{1 - \frac{\cos x}{\sin x}} \\ &= \frac{\cos^2 x}{\cos x - \sin x} + \frac{\sin^2 x}{\sin x - \cos x} \\ &= \frac{\cos^2 x - \sin^2 x}{\cos x - \sin x} \\ &= \frac{(\cos x - \sin x)(\cos x + \sin x)}{(\cos x - \sin x)} \\ &= \cos x + \sin x = \text{RHS} \\ &\therefore \text{Option (b) is correct.}\end{aligned}$$

11. Point of contact

12. 120°

13. $4\pi r^2$

14. $A = \frac{\alpha + \beta}{2}$ and $\alpha\beta = G^2$

$$\Rightarrow \alpha + \beta = 2A \text{ and } \alpha\beta = G^2$$

Quadratic equation whose roots are α and β is $x^2 - 2Ax + G^2 = 0$

$$\Rightarrow x^2 - 2Ax + G^2 = 0$$

OR

We have $ax^2 + bx + c = 0$

For equal roots

$$b^2 - 4ac = 0$$

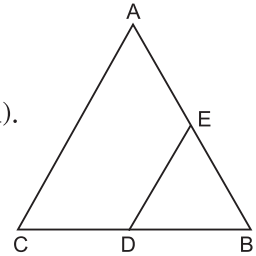
$$c = \frac{b^2}{4a}$$

15. Trigonometry

16. Given $BD = \frac{1}{2}BC \Rightarrow 2BD = BC$

Also, $\triangle ABC \sim \triangle BDE$ (both triangles are equilateral triangles, given).

$$\begin{aligned} \frac{\text{Area of } \triangle ABC}{\text{Area of } \triangle BDE} &= \frac{BC^2}{BD^2} \\ &= \frac{(2BD)^2}{BD^2} = \frac{4BD^2}{BD^2} = \frac{4}{1} \end{aligned}$$



17. $(\alpha - \beta)$, $(\beta - \gamma)$ are roots of equation $ax^2 + bx + c = 0$

$$\therefore (\alpha - \beta) + (\beta - \gamma) = \frac{-b}{a} \text{ and } (\alpha - \beta)(\beta - \gamma) = \frac{c}{a}$$

$$(\alpha - \gamma) = \frac{-b}{a} \text{ and } (\alpha - \beta)(\beta - \gamma) = \frac{c}{a}$$

$$\Rightarrow (\gamma - \alpha) = \frac{b}{a}$$

$$\text{We have, } \frac{(\alpha - \beta)(\beta - \gamma)}{\gamma - \alpha} = \frac{\frac{c}{a}}{\frac{b}{a}} = \frac{c}{a} \times \frac{a}{b} = \frac{c}{b}$$

OR

For coincident roots $D = 0$

$$\therefore [-(2 + m)]^2 - 4[1][-m^2 - 4m - 4] = 0$$

$$4 + m^2 + 4m + 4m^2 + 16m + 16 = 0$$

$$5m^2 + 20m + 20 = 0$$

$$m^2 + 4m + 4 = 0$$

$$\Rightarrow (m + 2)^2 = 0$$

$$\Rightarrow m = -2$$

18. Mean weight of 9 students = 19 kg

$$\Rightarrow \text{Total weight of 9 students} = 19 \times 9 = 171 \text{ kg}$$

A boy of 29 kg is added to group

$$\Rightarrow \text{Total weight of 10 students} = (171 + 29) \text{ kg} = 200 \text{ kg}$$

$$\Rightarrow \text{Mean weight of 10 students} = \frac{200}{10} = 20 \text{ kg}$$

\therefore The mean weight = 20 kg

19. Volume of each cube = 216 cm^3

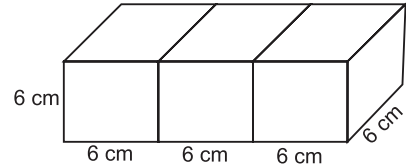
$$\text{Side of each cube} = 6 \text{ cm}$$

If cubes are joined together, it becomes a cuboid.

$$\text{Length of cuboid} = l = 18 \text{ cm}$$

$$\text{Breadth of cuboid} = b = 6 \text{ cm}$$

$$\text{Height of cuboid} = h = 6 \text{ cm}$$



$$\begin{aligned} \text{Total surface area of cuboid} &= 2[l \times b + b \times h + h \times l] \\ &= 2[18 \times 6 + 6 \times 6 + 6 \times 18] \\ &= 2[108 + 36 + 108] \\ &= 2[252] \\ &= 504 \text{ cm}^2 \end{aligned}$$

20. $[\sin^2 5^\circ + \sin^2 85^\circ] + [\sin^2 10^\circ + \sin^2 80^\circ] + [\sin^2 15^\circ + \sin^2 75^\circ] + [\sin^2 20^\circ + \sin^2 70^\circ] +$
 $[\sin^2 25^\circ + \sin^2 65^\circ] + [\sin^2 30^\circ + \sin^2 60^\circ] + [\sin^2 35^\circ + \sin^2 55^\circ] + [\sin^2 40^\circ + \sin^2 50^\circ] +$
 $(\sin^2 45^\circ) + (\sin^2 90^\circ)$

$$\begin{aligned} &= [\sin^2 5^\circ + \cos^2 5^\circ] + [\sin^2 10^\circ + \cos^2 10^\circ] + [\sin^2 15^\circ + \cos^2 15^\circ] + [\sin^2 20^\circ + \cos^2 20^\circ] \\ &+ [\sin^2 25^\circ + \cos^2 25^\circ] + [\sin^2 30^\circ + \cos^2 30^\circ] + [\sin^2 35^\circ + \cos^2 35^\circ] + [\sin^2 40^\circ + \cos^2 40^\circ] + \\ &[\sin^2 45^\circ + \sin^2 90^\circ] \\ &= 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + 1 + \frac{1}{\sqrt{2}} + 1 = 9 + \frac{1}{\sqrt{2}} \end{aligned}$$

21. Numbers are 105 and 84

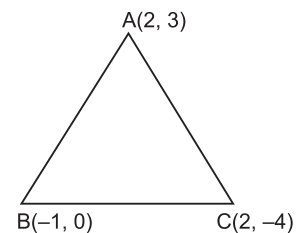
Using Euclid's division algorithm

$$105 = 84 \times 1 + 21$$

$$84 = 21 \times 4 + 0$$

\therefore HCF = 21

22. Area of $\triangle ABC = \frac{1}{2} |x_1(y_2 - y_3) + x_2(y_3 - y_1) + x_3(y_1 - y_2)|$
 $= \frac{1}{2} |2(0 - (-4)) + (-1)(-4 - 3) + 2(3 - 0)|$
 $= \frac{1}{2} |8 + 7 + 6| = \frac{21}{2} \text{ sq units.}$



23. Total number of ways to draw a card = 52

(i) Number of black face cards = 6

$$\therefore \text{Required probability} = \frac{6}{52} = \frac{3}{26}$$

(ii) Number of red face cards = 6

$$\text{Required probability} = \frac{6}{52} = \frac{3}{26}$$

24. $2x + 3y = 9$...*(i)*

$3x + 4y = 5$...*(ii)*

From equation (i) we get

$$x = \frac{9 - 3y}{2}$$
 ...*(iii)*

Substituting in equation (ii) we get

$$3\left(\frac{9 - 3y}{2}\right) + 4y = 5$$

$$\Rightarrow 27 - 9y + 8y = 10$$

$$y = 17$$

When $y = 17$, equation (iii) becomes

$$x = \frac{9 - 51}{2} = -21$$

$$\therefore x = -21, y = 17$$

OR

$7x + 11y - 3 = 0$...*(i)*

$8x + y - 15 = 0$...*(ii)*

From equation (ii) we get

$$y = 15 - 8x$$
 ...*(iii)*

Substituting in equation (i) we get

$$7x + 11(15 - 8x) - 3 = 0$$

$$7x + 165 - 88x - 3 = 0$$

$$81x = 162$$

$$x = 2$$

When $x = 2$, equation (iii) becomes

$$y = 15 - 8 \times 2 = -1$$

$$\therefore x = 2, y = -1$$

25. $A + B = 90^\circ \Rightarrow B = 90^\circ - A$...*(i)*

Now $\cot B = \cot(90^\circ - A) = \tan A$ [using (i)]

$$\Rightarrow \cot B = \frac{3}{4}$$

OR

$$\tan 10^\circ \cdot \tan 75^\circ \cdot \tan 15^\circ \cdot \tan 80^\circ$$

$$= \cot(90^\circ - 10^\circ) \cdot \cot(90^\circ - 75^\circ) \cdot \tan 15^\circ \cdot \tan 80^\circ$$

$$= \cot 80^\circ \times \cot 15^\circ \times \frac{1}{\cot 15^\circ} \times \frac{1}{\cot 80^\circ} = 1$$

26. In $\triangle ABC$ and $\triangle ADE$

$$\therefore DE \parallel BC$$

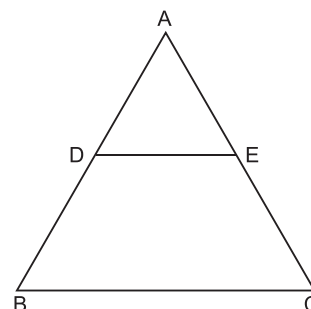
$$\angle ADE = \angle ABC \text{ (corresponding angles)}$$

$$\angle AED = \angle ACB \text{ (corresponding angles)}$$

$$\therefore \angle A = \angle A \text{ (common)}$$

$$\therefore \triangle ADE \sim \triangle ABC$$

(SAS)



$$\Rightarrow \frac{AD}{AB} = \frac{DE}{BC}$$

$$\Rightarrow \frac{3}{AD + DB} = \frac{6}{BC}$$

$$\frac{3}{3 + 2} = \frac{6}{BC} \Rightarrow BC = \frac{6 \times 5}{3}$$

$$\Rightarrow BC = 10 \text{ cm}$$

27. The bells will toll together at an interval of 9, 12 and 15 minutes.

$$9 = 3^2, 12 = 2^2 \times 3, 15 = 3 \times 5$$

$$\therefore \text{LCM}(9, 12, 15) = 3^2 \times 2^2 \times 5 = 180$$

\therefore Bells will toll together after 180 minutes.

28. $x + 2y - 7 = 0$...*(i)*

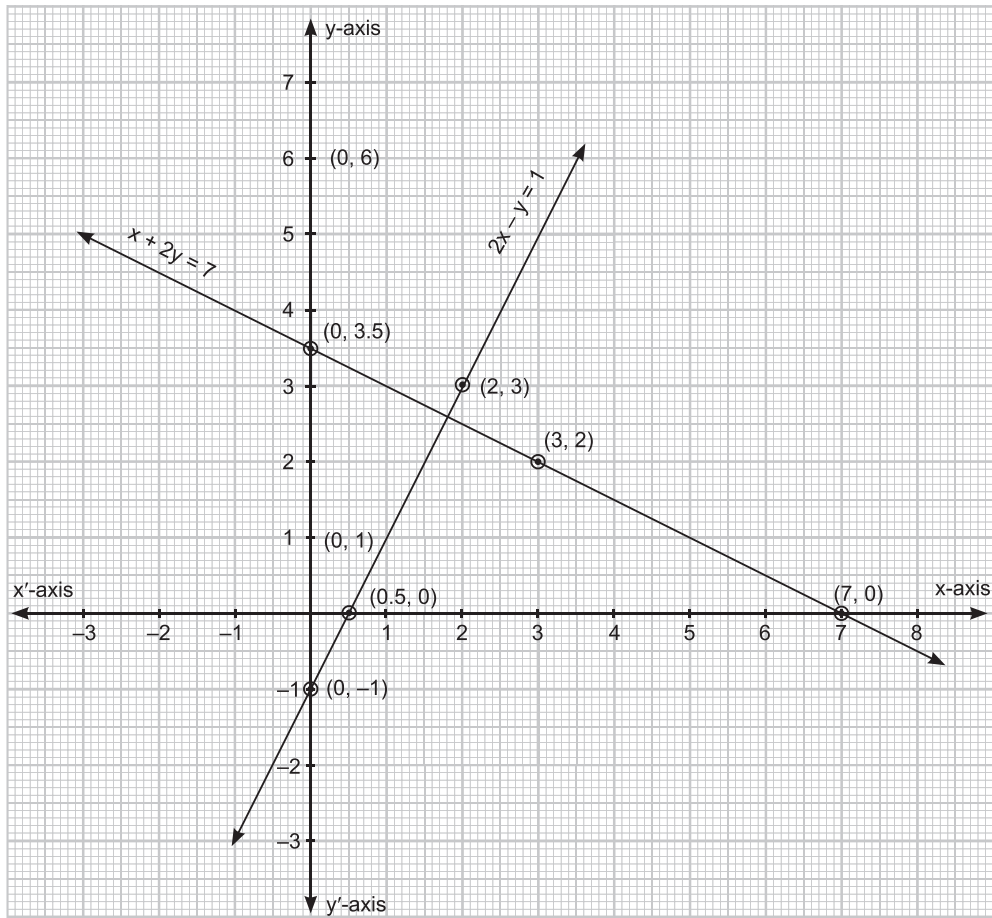
$$2x - y - 1 = 0 \text{ ...}(ii)$$

Table for equation *(i)*

x	7	0	3
y	0	3.5	2

Table for equation *(ii)*

x	0.5	0	2
y	0	-1	3



Points meet at y-axis at (0, 3.5) and (0, -1).

- 29.** The coordinates of house be H(2, 4) and office be O(13, 26)

Distance between house to office

$$\begin{aligned} HO &= \sqrt{(13 - 2)^2 + (26 - 4)^2} \\ &= \sqrt{(11)^2 + (22)^2} \\ HO &= \sqrt{121 + 484} \\ &= \sqrt{605} \\ HO &= 11\sqrt{5} \text{ km} \end{aligned}$$

The coordinates of bank and school respectively B(5, 8) and S(13, 14)

$$\begin{aligned} HB &= \sqrt{(5 - 2)^2 + (8 - 4)^2} \\ &= \sqrt{9 + 16} \\ &= \sqrt{25} \\ &= 5 \text{ km} \\ BS &= \sqrt{(13 - 5)^2 + (14 - 8)^2} \\ &= \sqrt{64 + 36} = \sqrt{100} \\ &= 10 \text{ km} \end{aligned}$$

$$SO = \sqrt{(13-13)^2 + (26-14)^2}$$

$$= \sqrt{(12)^2} = 12\text{km}$$

$$\text{Total distance} = 5\text{km} + 10\text{km} + 12\text{km}$$

$$= 27\text{km}$$

$$\text{Extradistance travelled} = (27 - 11\sqrt{5})\text{km}$$

$$= 27 - 11(2.236)$$

$$= 27 - 24.596$$

$$= 2.404\text{km}$$

30. $(\sin A + \cos A) \sec A = (\sin A + \cos A) \times \frac{1}{\cos A} = \frac{\sin A + \cos A}{\cos A}$

$$= \frac{\sin A}{\cos A} + \frac{\cos A}{\cos A}$$

$$= \tan A + 1 = \frac{5}{12} + 1 = \frac{17}{12}$$

31. **Given:** Two parallel tangents to a circle with centre O. Tangent AB with point of contact C intersects XY at A and X'Y' at B.

To Prove: $\angle AOB = 90^\circ$

Construction: Join OA, OB and OC

Proof: In $\triangle AOP$ and $\triangle AOC$

$$AP = AC \quad \text{[Lengths of tangents from common point]}$$

$$OP = OC \quad \text{[Radii]}$$

$$OA = OA \quad \text{[Common]}$$

$$\Rightarrow \triangle AOP \cong \triangle AOC \quad \text{[SSS congruence rule]}$$

$$\Rightarrow \angle PAO = \angle CAO \quad \text{[C.P.C.T.]}$$

$$\therefore \angle PAC = 2\angle OAC \quad \dots(i)$$

Similarly $\angle QBC = 2\angle OBC \quad \dots(ii)$

Adding (i) and (ii), we get

$$\angle PAC + \angle QBC = 2[\angle OAC + \angle OBC]$$

$$\angle PAC + \angle QBC = 180^\circ$$

[interior consecutive angles on same side of transversal]

$$2[\angle OAC + \angle OBC] = 180^\circ$$

$$\Rightarrow \angle OAC + \angle OBC = 90^\circ$$

$$\text{In } \triangle AOB, \angle AOB + \angle OAC + \angle OBC = 180^\circ$$

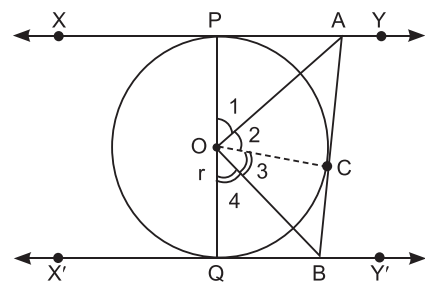
$$\Rightarrow \angle AOB + 90^\circ = 180^\circ \Rightarrow \angle AOB = 90^\circ$$

OR

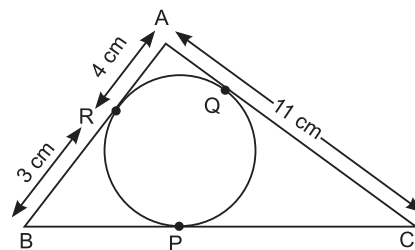
$$BR = BP \quad \text{(lengths of tangents from B)}$$

$$\therefore BP = 3\text{cm}$$

Similarly $AR = AQ$



\Rightarrow $AQ = 4 \text{ cm}$
 $QC = AC - AQ = 11 - 4 = 7 \text{ cm}$
 Also $QC = PC$
 $\Rightarrow PC = 7 \text{ cm}$
 Now $BC = BP + PC = 3 + 7 = 10 \text{ cm}$



32. Given: In $\triangle ABC$, $AB \perp BC$ and $DE \perp AC$

To prove: $\triangle ABC \sim \triangle AED$.

Proof: In $\triangle AED$ and $\triangle ABC$

$$\angle AED = \angle ABC$$

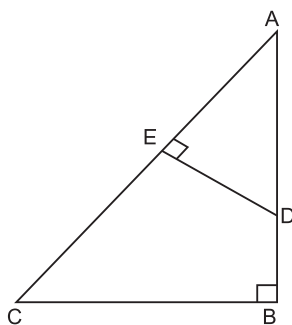
(each 90°)

$$\angle A = \angle A$$

(common)

$$\therefore \triangle AED \sim \triangle ABC$$

(AA corollary)



OR

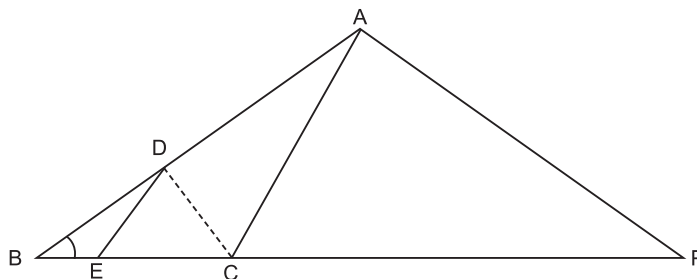
Given: In $\triangle ABC$, $DE \parallel AC$

$$\frac{BE}{EC} = \frac{BC}{CP}$$

...(i)

To prove:

$$DC \parallel AP$$



Construction: Join DC

Proof: In $\triangle ACB$,

$$DE \parallel AC$$

(given)

\therefore

$$\frac{BE}{EC} = \frac{BD}{AD}$$

...(i) (By BPT)

Also,

$$\frac{BE}{EC} = \frac{BC}{CP}$$

...(ii) (Given)

From (i) and (ii)

$$\frac{BD}{AD} = \frac{BC}{CP}$$

In $\triangle ABP$,

$$\frac{BD}{AD} = \frac{BC}{CP}$$

(proved)

$$CD \parallel AP$$

(Using converse of B.P.T.)

33. $OA = 7$ cm

$$\begin{aligned} OB &= OA + AB \\ &= 7 + 21 = 28 \text{ cm} \end{aligned}$$

$$\angle AOD = \theta = 30^\circ$$

$$\begin{aligned} \text{Area of sector AOD} &= \frac{\theta}{360^\circ} \times \pi r^2 \\ &= \frac{30}{360} \times \pi \times 7 \times 7 \quad (r = 7 \text{ cm}) \\ &= \frac{49\pi}{12} \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{Area of sector BOC} &= \frac{30}{360} \times \pi \times 28 \times 28 \quad (r = 28 \text{ cm}) \\ &= \frac{196\pi}{3} \text{ cm}^2 \end{aligned}$$

$$\begin{aligned} \text{(shaded area) Area swept by wiper} &= \left(\frac{196\pi}{3} - \frac{49\pi}{12} \right) \text{ cm}^2 = \left(\frac{784 - 49}{12} \right) \pi \text{ cm}^2 \\ &= \frac{735}{12} \pi = \frac{245}{4} \pi \text{ cm}^2 \end{aligned}$$

OR

OR is diameter of circle

ΔQPR is a right-angled triangle

$$\begin{aligned} \therefore QR^2 &= PQ^2 + PR^2 \\ &= (24)^2 + (7)^2 = 576 + 49 \end{aligned}$$

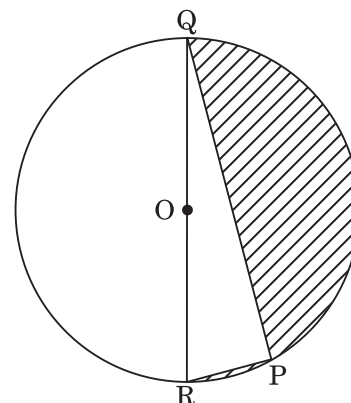
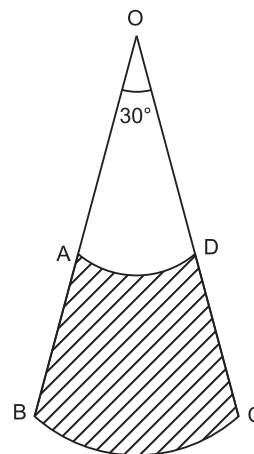
$$QR^2 = 625$$

$$QR = 25 \text{ cm}$$

$$\therefore OR = \frac{1}{2} QR = \frac{25}{2} \text{ cm.}$$

Area of shaded region = area of semicircle – area of ΔPQR

$$\begin{aligned} &= \frac{\pi \left(\frac{25}{2} \right)^2}{2} - \frac{1}{2} \times 7 \times 24 \\ &= \frac{22}{7} \times \frac{1}{2} \times \frac{625}{4} - 84 \\ &= \left(\frac{6875}{28} - 84 \right) \text{ cm}^2 \\ &= (245.53 - 84) \text{ cm}^2 \\ &= 161.53 \text{ cm}^2 \end{aligned}$$



34.

Life time (in hours)	Frequency (f_i)	Class marks (x_i)	$u_i = \frac{x_i - a}{h}$	$f_i u_i$
0 – 20	10	10	– 2	– 20
20 – 40	35	30	– 1	– 35
40 – 60	52	50	0	0
60 – 80	61	70	1	61
80 – 100	38	90	2	76
100 – 120	29	110	3	87
Total	225			169

Here, $a = 50, h = 20$

We have,

$$\begin{aligned} \text{Mean} &= a + \frac{\sum f_i u_i}{\sum f_i} \times h \\ &= 50 + \frac{169}{225} \times 20 \\ &= 50 + \frac{3380}{225} = 50 + 15.02 = 65.02 \end{aligned}$$

Average life time of electrical components is 65.02

35. Let two successive integral multiples of 5 are $5x$ and $5(x+1)$

$$\begin{aligned} \therefore (5x)(5x + 5) &= 300 \\ 25x^2 + 25x &= 300 \\ x^2 + x - 12 &= 0 \\ x^2 + 4x - 3x - 12 &= 0 \\ (x + 4)(x - 3) &= 0 \end{aligned}$$

$$x = -4 \text{ (rejected) and } x = 3 \text{ (rejected)}$$

$$\text{1st integral of } 5 = 5 \times 3 = 15$$

$$\begin{aligned} \text{Next successive integral} &= 5(3 + 1) \\ &= 5 \times 4 = 20 \end{aligned}$$

OR

Let speed of the train = x km/hr

$$\text{Distance} = 360 \text{ km}$$

$$\text{Time taken} = \frac{360}{x} \text{ hr}$$

When speed = $(x + 10)$ km/hr

$$\text{Time taken} = \frac{360}{x + 10} \text{ hr}$$

$$\text{A.T.Q.} \quad \frac{360}{x} - \frac{360}{x + 10} = 3$$

$$360x + 3600 - 360x = 3x^2 + 30x$$

$$3x^2 + 30x - 3600 = 0$$

$$\begin{aligned} \Rightarrow \quad x^2 + 10x - 1200 &= 0 \\ (x + 40)(x - 30) &= 0 \\ x &= -40 \text{ or } x = 30 \end{aligned}$$

Rejecting $x = -40$ we get $x = 30$

\therefore Usual speed of the train = 30 km/hr

36. Let 1st term of the A.P. = a

Common difference = d

A.T.Q. $a_4 + a_8 = 24$

$$\Rightarrow a + 3d + a + 7d = 24$$

$$2a + 10d = 24$$

$$\Rightarrow a + 5d = 12 \quad \dots(i)$$

Also $a_6 + a_{10} = 44$

$$\Rightarrow a + 5d + a + 9d = 44$$

$$\Rightarrow 2a + 14d = 44$$

$$\Rightarrow a + 7d = 22 \quad \dots(ii)$$

Solving (i) and (ii)

$$a + 7d = 22$$

$$a + 5d = 12$$

$$- \quad - \quad -$$

$$2d = 10 \Rightarrow d = 5$$

When $d = 5$, eq. (i) becomes

$$a + 5 \times 5 = 12$$

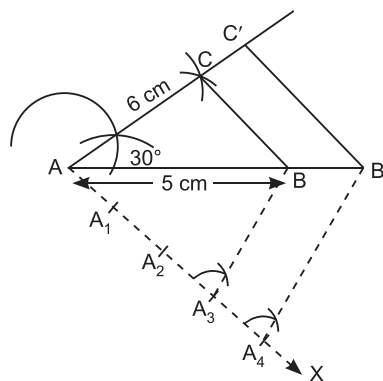
$$a = -13$$

$$a_1 = a = -13$$

$$a_2 = a + d = -13 + 5 = -8$$

$$a_3 = a + 2d = -13 + 10 = -3$$

37.



AC'B' is the required triangle.

38. Let kite is at K

AK = length of string = 54 m

BK = height of the kite above the ground

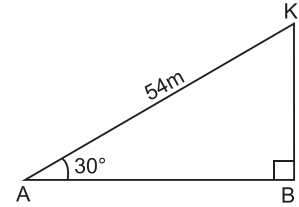
$$\angle KAB = 30^\circ$$

In right $\triangle KBA$,

$$\frac{KB}{AK} = \sin 30^\circ$$

$$\frac{KB}{54} = \frac{1}{2}$$

$$KM = 27 \text{ m}$$



\therefore Height of the kite above the ground = 27 m

39.

Age (in years)	Number of patients (f_i)	$c.f.$
0 – 10	22	22
10 – 20	10	32
20 – 30	8	40
30 – 40	15	55
40 – 50	5	60
50 – 60	6	66
Total	66	

$$N = 66, \frac{N}{2} = 33$$

Then median class is 20 – 30

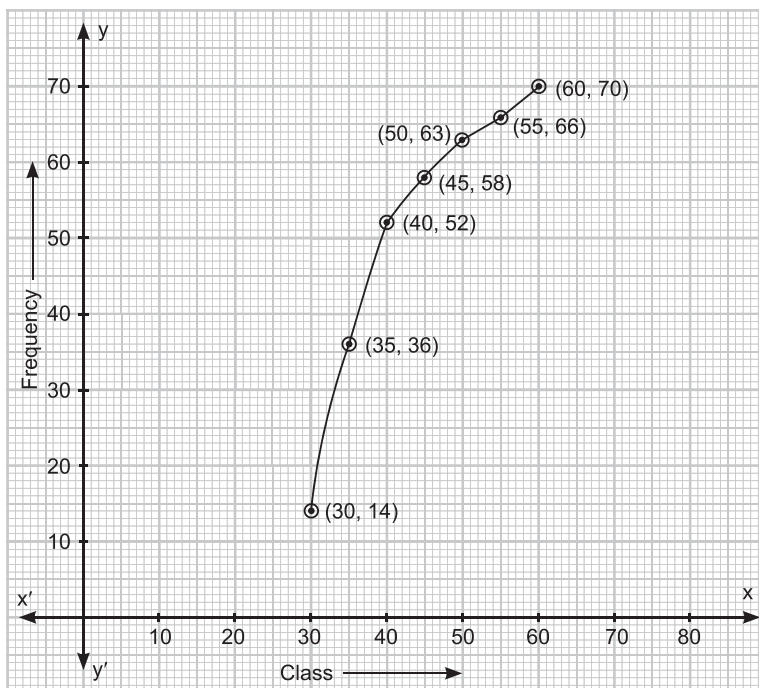
here, $l = 20, f = 8, c.f. = 32, h = 10$

$$\begin{aligned} \text{Median} &= l + \left(\frac{\frac{N}{2} - c.f.}{f} \right) \times h \\ &= 20 + \left(\frac{33 - 32}{8} \right) \times 10 \\ &= 20 + \frac{10}{8} \\ &= 20 + 1.25 \end{aligned}$$

$$\text{Median} = 21.25$$

OR

Classes	Frequency	$c.f.$	Points
25 – 30	14	14	(30, 14)
30 – 35	22	36	(35, 36)
35 – 40	16	52	(40, 52)
40 – 45	6	58	(45, 58)
45 – 50	5	63	(50, 63)
50 – 55	3	66	(55, 66)
55 – 60	4	70	(60, 70)



40. Radius of upper end

$$R = 20 \text{ cm}$$

$$\text{Radius of lower end } r = 8 \text{ cm}$$

$$\text{Height } (h) = 16 \text{ cm}$$

Let slant height = l cm

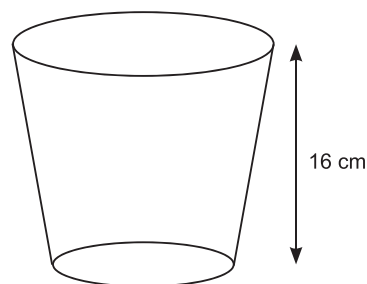
$$l = \sqrt{h^2 + (R - r)^2}$$

$$l = \sqrt{(16)^2 + (12)^2} = 20 \text{ cm}$$

$$\begin{aligned} \text{Area of metal sheet} &= \pi l(R + r) + \pi r^2 \\ &= \pi \times 20(20 + 8) + \pi \times 8^2 \\ &= 560\pi + 64\pi = 624\pi \text{ cm}^2 \end{aligned}$$

$$\text{Rate of metal sheet} = \frac{\text{₹ } 15}{100 \text{ cm}^2}$$

$$\begin{aligned} \text{Total cost} &= \text{₹ } 624 \pi \times \frac{15}{100} = \text{₹ } \frac{624 \times 22 \times 15}{7 \times 100} \\ &= \text{₹ } 294.17 \text{ (app.)} \end{aligned}$$



OR

$$\text{Radius of upper end} = R_1 = \frac{40}{2} = 20 \text{ cm}$$

$$\text{Radius of lower end} = R_2 = \frac{20}{2} = 10 \text{ cm}$$

Let height be h cm

$$\text{Volume of bucket} = 17600 \text{ cm}^3$$

$$\Rightarrow \frac{1}{3} \pi h (R_1^2 + R_2^2 + R_1 R_2) = 17600$$

$$\Rightarrow \frac{1}{3} \times \frac{22}{7} \times h [(20)^2 + (10)^2 + 20 \times 10] = 17600$$

$$\Rightarrow h = \frac{17600 \times 7 \times 3}{22 \times 700} = 24 \text{ cm}$$

Now slant height of bucket

$$l = \sqrt{h^2 + (R_1 - R_2)^2}$$

$$l = \sqrt{(24)^2 + (10)^2} = \sqrt{676} = 26 \text{ cm}$$

$$\text{Total surface area} = \pi R_2^2 + \pi l (R_1 + R_2)$$

$$= \pi [(10)^2 + 26 (20 + 10)]$$

$$= \frac{22}{7} \times 880 \text{ cm}^2 = 2765.714 \text{ cm}^2$$